

Introduction to arc spaces

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Abstract: I will give an introduction to the arc space attached to a singularity. In the first one I will give motivation, definitions and basic results. In particular I will talk about the truncation maps and cylinders of the space of arcs. In the second one I will talk about the Nash problem which relates the arc space and the resolutions and minimal model of the singular space.

References

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